

# Optimal Planning and Shortcut Learning: An Unfulfilled Promise

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# Outline

- 1 Background
- 2 Learning Shortcut Rules
- 3 Empirical Evaluation



# STRIPS

- A STRIPS planning problem with action costs is a 5-tuple  $\Pi = \langle P, s_0, G, A, C \rangle$ 
  - $P$  is a set of boolean propositions
  - $s_0 \subseteq P$  is the initial state
  - $G \subseteq P$  is the goal
  - $A$  is a set of actions.
  - Each action is a triple  $a = \langle \text{pre}(a), \text{add}(a), \text{del}(a) \rangle$
  - $C : A \rightarrow \mathbb{R}^{0+}$  assigns a cost to each action
- Applying action sequence  $\rho = \langle a_0, a_1, \dots, a_n \rangle$  at state  $s$  leads to  $s[[\rho]]$
- The cost of action sequence  $\rho$  is  $\sum_{i=0}^n C(a_i)$



# Intended Effects

Chicken logic

Why did the chicken cross the road?

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Why did the chicken cross the road?

To get to the other side

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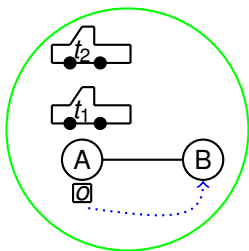
## Observation

Every action along an optimal plan is there for a reason

- Achieve a precondition for another action
- Achieve a goal



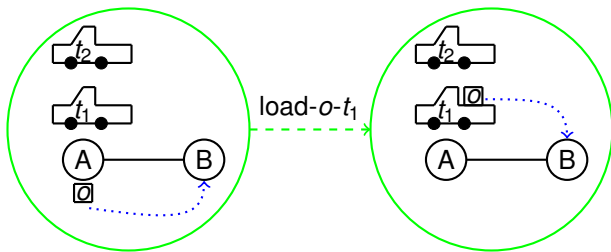
# Intended Effects — Example



- If  $\langle \text{load-}o\text{-}t_1 \rangle$  is the beginning of an optimal plan, then:
  - There must be a reason for applying  $\text{load-}o\text{-}t_1$
  - $\text{load-}o\text{-}t_1$  achieves  $o\text{-in-}t_1$
  - Any continuation of this path to an optimal plan must use some action which requires  $o\text{-in-}t_1$



# Intended Effects — Example

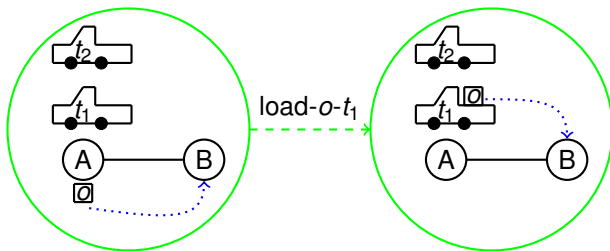


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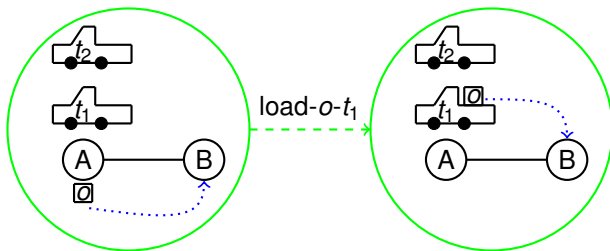
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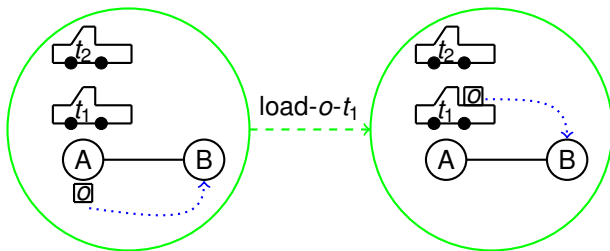
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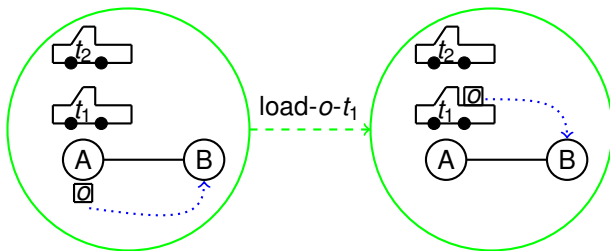
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# Intended Effects — Formal Definition

## Intended Effects

Given a path  $\pi = \langle a_0, a_1, \dots, a_n \rangle$  a set of propositions  $X \subseteq s_0 [[\pi]]$  is an **intended effect of  $\pi$**  iff there exists a path  $\pi'$  such that  $\pi \cdot \pi'$  is an optimal plan and  $\pi'$  consumes exactly  $X$ , i.e.,  
( $p \in X$  iff there is a causal link  $\langle a_i, p, a_j \rangle$  in  $\pi \cdot \pi'$ , with  $a_i \in \pi$  and  $a_j \in \pi'$ ).

- $IE(\pi)$  — the set of all intended effect of  $\pi$



# Intended Effects: Complexity

## Hard to Find Exactly

It is P-SPACE Hard to find the intended effects of path  $\pi$ .

## Sound Approximation

We can use supersets of  $IE(\pi)$  to derive constraints about any continuation of  $\pi$ .



# Shortcuts and Approximate Intended Effects

## Intuition

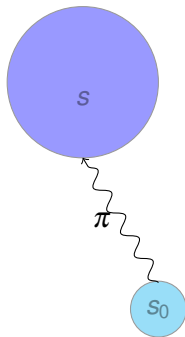
$X$  can not be an intended effect of  $\pi$  if there is a cheaper way to achieve  $X$



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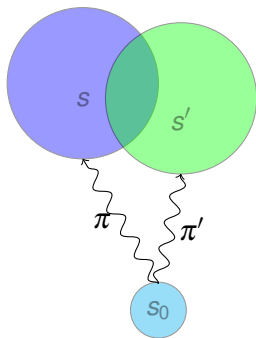




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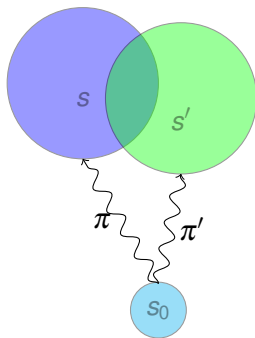
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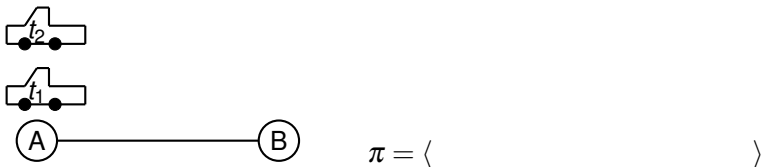


$$C(\pi') < C(\pi)$$

Any continuation of  $\pi$  into an optimal plan must use some fact in  $s \setminus s'$



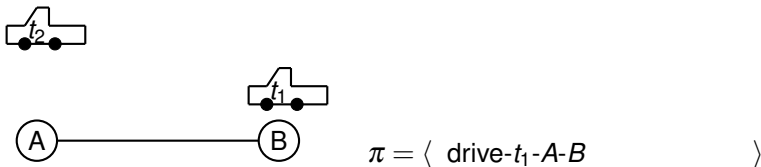
# Shortcuts and Approximate Intended Effects: Example



- $t_2$ -at- $B$  can not be an intended effect of  $\pi$  — we must use  $t_1$ -at- $B$
- $t_1$ -at- $B$  can not be an intended effect of  $\pi$  — we must use  $t_2$ -at- $B$

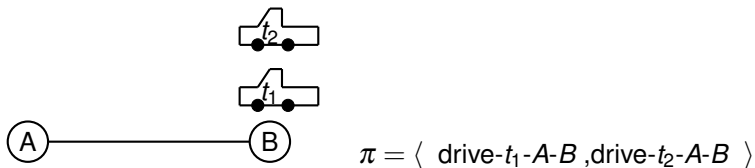


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- $t_2\text{-at-}B$  can not be an intended effect of  $\pi$  — we must use  $t_1\text{-at-}B$
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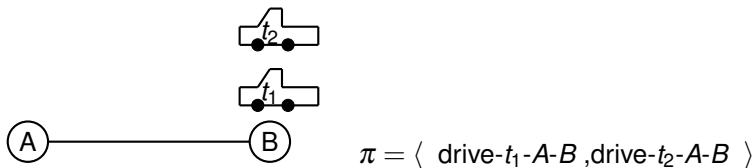
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# Shortcuts and Approximate Intended Effects: Example

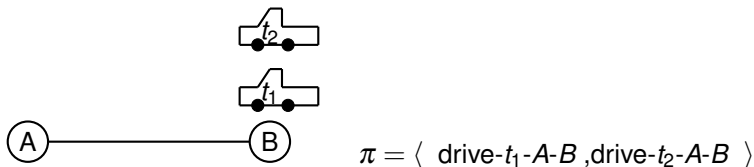


$$\pi' = \langle \text{drive-}t_2\text{-}A\text{-}B \rangle$$

- $t_2\text{-at-}B$  can not be an intended effect of  $\pi$  — we must use  $t_1\text{-at-}B$
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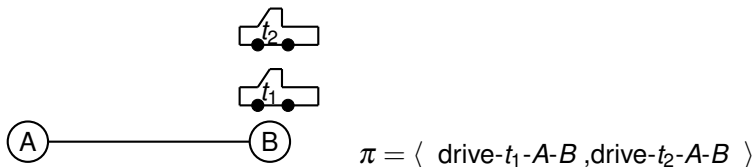


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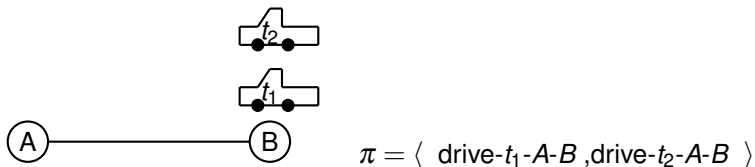
$$\pi'' = \langle \text{drive-}t_1\text{-}A\text{-}B \rangle$$

- $t_1\text{-at-}B$  can not be an intended effect of  $\pi$  — we must use  $t_2\text{-at-}B$





# Shortcuts and Approximate Intended Effects: Example



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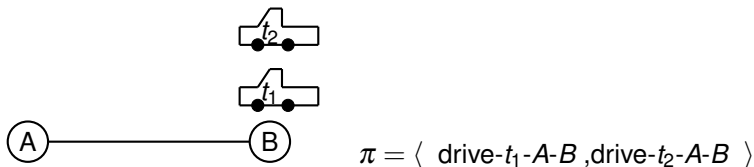
- $t_2\text{-at-}B$  can not be an intended effect of  $\pi$  — we must use  $t_1\text{-at-}B$

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# Shortcuts and Approximate Intended Effects: Example



$$\pi' = \langle \text{drive-}t_2\text{-}A\text{-}B \rangle$$

- $t_2\text{-at-}B$  can not be an intended effect of  $\pi$  — we must use  $t_1\text{-at-}B$

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- $t_1\text{-at-}B$  can not be an intended effect of  $\pi$  — we must use  $t_2\text{-at-}B$

We must use both  $t_1\text{-at-}B$  and  $t_2\text{-at-}B$

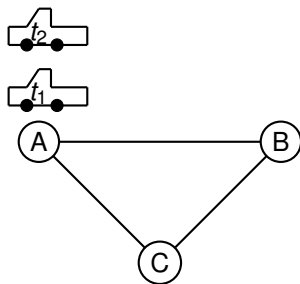


# Finding Shortcuts

- Where do the shortcuts come from?
- They can be dynamically generated for each path
- Our previous paper used the **causal structure** of the current path — a graph whose nodes are action occurrences, with an edge from  $a_i$  to  $a_j$  if there is a causal link where  $a_i$  provides some proposition for  $a_j$
- Previous shortcut rules attempted to remove some actions, according to the the causal structure, to obtain a shortcut



# Shortcuts Example

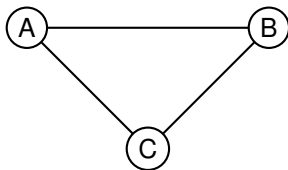


Causal Structure

$\pi = \langle \quad \quad \quad \rangle$



# Shortcuts Example



drive- $t_1$ -A-B

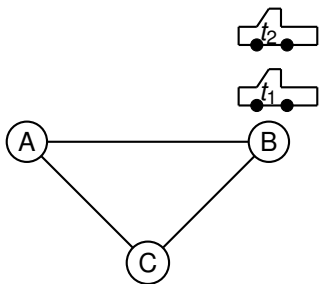
Causal Structure

$\pi = \langle$  drive- $t_1$ -A-B

$\rangle$



## Shortcuts Example



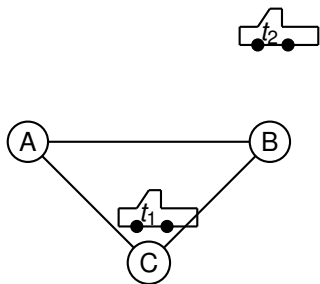
Causal Structure

drive- $t_1$ -A-Bdrive- $t_2$ -A-B

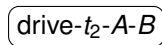
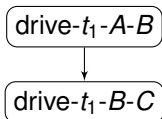
$$\pi = \langle \text{drive-}t_1\text{-A-B}, \text{drive-}t_2\text{-A-B} \rangle$$



## Shortcuts Example

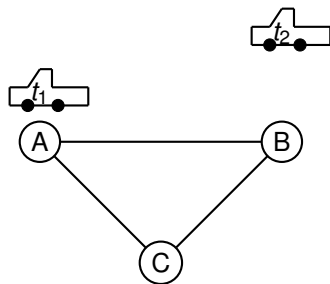


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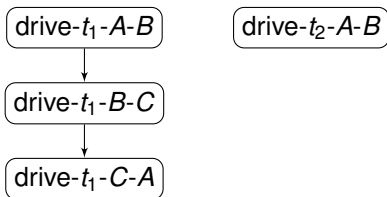


$$\pi = \langle \text{drive-}t_1\text{-A-B}, \text{drive-}t_2\text{-A-B}, \text{drive-}t_1\text{-B-C} \rangle$$

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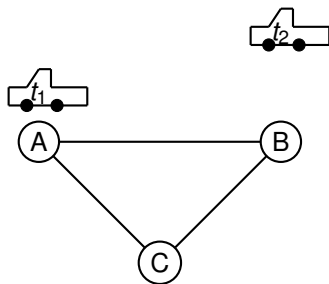
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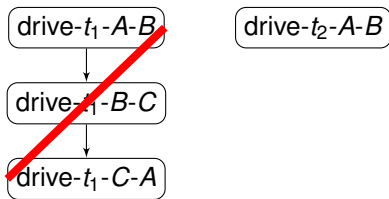
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## Shortcuts Example



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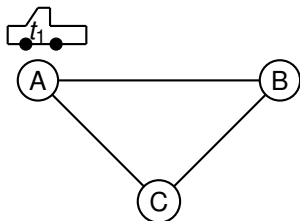
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$$\pi' = \langle \text{drive-}t_2\text{-A-B} \rangle$$



# Shortcut Rules that Add Actions

- The previous shortcut rules only remove actions from  $\pi$



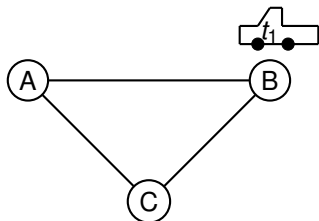
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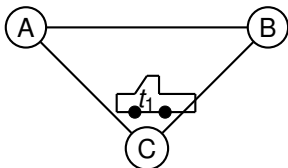
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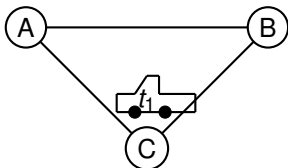
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# Learning Shortcut Rules that Add Actions

- We developed techniques for learning shortcut rules that add new actions

## Spoiler

These shortcut rules do not improve performance



# When to Learn

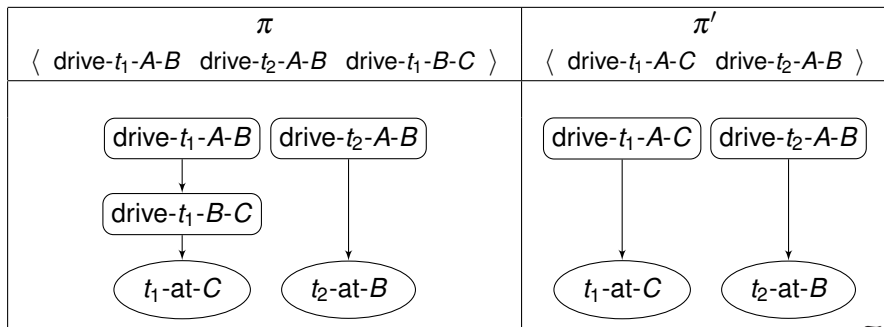
- Recall that a good shortcut  $\pi'$  achieves almost everything the original path  $\pi$  did
- In the extreme:  $\pi'$  achieves everything  $\pi$  achieved
- The search algorithm detects when this happens — when a new path to an existing state is detected
- We learn whenever we have two paths reaching the same state, regardless of whether the new path is cheaper or not





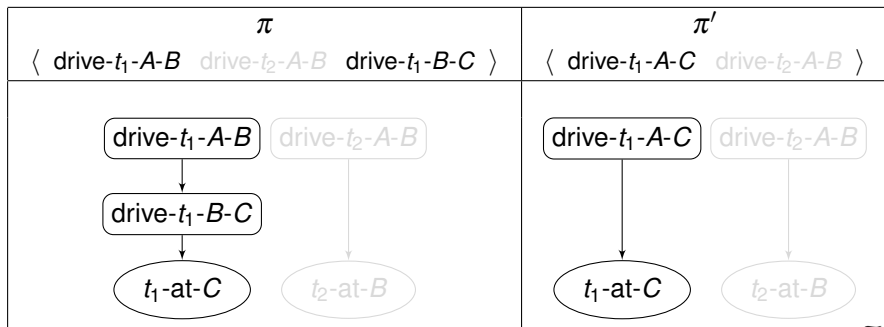
# How to Learn

- The input to our learning algorithm is two paths reaching the same state
- Instead of looking at the state as a whole, we look at individual facts, and the causal structure leading to each fact



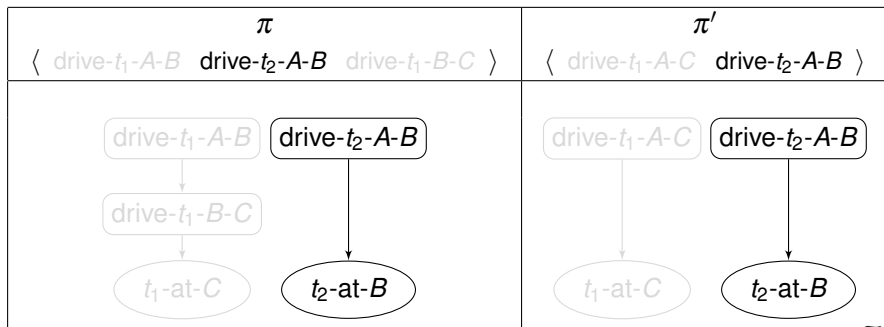
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# Shortcut Rules

- From the pair of partial paths reaching each fact, we learn a new shortcut rule
- Shortcut rules are used when a path  $\pi$  is evaluated, as follows:
  - 1 Each shortcut rule is checked for applicability
  - 2 If it is applicable, a set of shortcuts is generated
  - 3 From each such shortcut, an  $\exists$ -opt landmark is derived
- Three types of shortcut rules, which differ in the details of these steps



# Concrete Shortcut Rule

Rule

$\langle \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle \leftarrow \langle \text{drive-}t_1\text{-}A\text{-}C \rangle$

# Concrete Shortcut Rule

## Rule

$$\langle \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle \leftarrow \langle \text{drive-}t_1\text{-}A\text{-}C \rangle$$

## Example 1

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$

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$$\langle \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle \leftarrow \langle \text{drive-}t_1\text{-}A\text{-}C \rangle$$

## Example 1

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$

## Example 2

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_2\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle$$


# Concrete Shortcut Rule

## Rule

$$\langle \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle \leftarrow \langle \text{drive-}t_1\text{-}A\text{-}C \rangle$$

## Example 1

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$

## Example 2

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_2\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle$$


# Concrete Shortcut Rule

## Rule

$$\langle \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle \leftarrow \langle \text{drive-}t_1\text{-}A\text{-}C \rangle$$

## Example 1

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$

## Example 2

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_2\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle$$

Not applicable



# Unordered Shortcut Rule

## Rule

$$\{\text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C\} \leftarrow \{\text{drive-}t_1\text{-}A\text{-}C\}$$

## Example 1

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$

## Example 2

$$\pi = \langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}B, \text{drive-}t_2\text{-}A\text{-}B, \text{drive-}t_1\text{-}B\text{-}C \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C \rangle$$
$$\langle \text{drive-}t_2\text{-}C\text{-}A, \text{drive-}t_1\text{-}A\text{-}C, \text{drive-}t_2\text{-}A\text{-}B \rangle$$


# Generalized Shortcut Rule

## Rule

$$\{\text{drive-}T\text{-}X\text{-}Y, \text{drive-}T\text{-}Y\text{-}Z\} \leftarrow \{\text{drive-}T\text{-}X\text{-}Z\}$$

## Example 1

$$\pi = \langle \text{drive-}t_1\text{-}B\text{-}C, \text{drive-}t_2\text{-}A\text{-}B, \text{drive-}t_1\text{-}C\text{-}A \rangle$$
$$\langle \text{drive-}t_1\text{-}B\text{-}A, \text{drive-}t_2\text{-}A\text{-}B \rangle$$


# The Utility Problem

- Checking if a shortcut rule is applicable takes time
- Sometimes, this applicability check says the rule is not applicable
- This is the well known utility problem
  
- We address it by keeping counts of how many times each rule was checked for applicability, and how many times it was applicable
- Low utility shortcut rules are discarded



# Outline

- 1 Background
- 2 Learning Shortcut Rules
- 3 Empirical Evaluation**





# Coverage

Shortcut Rules	Solved Problems
<b>none</b>	<b>661</b>
<b>concrete</b>	609
<b>unordered</b>	585
<b>generalized</b>	487

- None of the shortcut rules solve more problems than no shortcuts in any domain



# Expansions

Shortcut Rules	Total Expanded States
<b>none</b>	3785517
<b>concrete</b>	3758042
<b>unordered</b>	<b>3736052</b>
<b>generalized</b>	3777860

- The reduction in total number of expanded state for commonly solved problems is about 1%



# Discussions

- Possible reasons for failure:
  - Concrete shortcut rules are too strict
  - Unordered and generalized shortcut rules generate too many possible shortcuts, and we only look at some of them
  - The base heuristic ( $\exists$ -opt and regular landmarks) is already very powerful
- Future work:
  - Exploit the partial order information from the causal structure
  - Smarter ways of applying unordered/generalized shortcut rules
  - Inter-problem learning with generalized shortcut rules
  - [Insert your idea here](#)



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# Thank You

